

$$\hat{n} = n + ik$$

$r = \frac{1 - \hat{n}}{1 + \hat{n}}$ can get phase shift from relative values of...

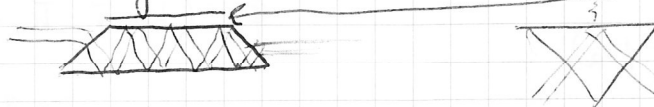
for glass, the critical angle is 43° , at 45° get total internal reflection

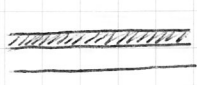
$$\alpha = \frac{2\pi}{\lambda} \sqrt{\frac{\sin^2 \theta}{n^2} - 1} = \frac{2\pi}{\lambda} \sqrt{\frac{1}{2}(1.5)^2 - 1} = \frac{2\pi}{\lambda} \sqrt{1.125 - 1} = \frac{2\pi}{500} (0.35) = \frac{2.2}{500} \text{ nm}^{-1}$$

$$k'' \rightarrow \frac{2\pi}{\lambda} \cdot n_{\text{air}} \text{ for } k'' \approx 1 \quad \alpha = \frac{2.2}{500} = 0.0044 \text{ nm}^{-1}$$

at a steeper angle $\alpha \uparrow \Rightarrow \lambda \downarrow$ smaller maximum effect

evanescent fields are used to sample materials: monolayer of material IR spectroscopy

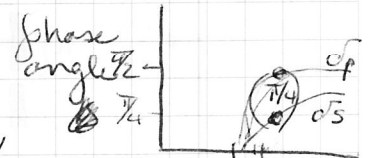


interference layers  $n_{\text{film}} \sim \sqrt{n_{\text{glass}}}$ $d \sim \frac{\lambda}{4}$

apply same Boundary Conditions \Rightarrow 4% reflection \rightarrow 99% transmission w/o film

multilayered films for low reflectors or high reflectors (high + low n coatings)

$$r_s = \frac{\cos \theta - i \sqrt{\sin^2 \theta - n^2}}{\cos \theta + i \sqrt{\sin^2 \theta - n^2}}$$



for glass take $n = \frac{1}{1.5}$ in $\tan(\Delta/2) = \cos \theta \sqrt{\sin^2 \theta - n^2} / \sin \theta$ fresnel rhomb

gives you a phase shift of $\pi/4$ (45°) when cut $\sim 46^\circ$ because of the relative phase shift \$500

used to make circular polarized light fresnel rhomb

Reflection or Transmission Matrix $\begin{bmatrix} A' \\ B' \end{bmatrix} = \begin{bmatrix} -\frac{1-n}{1+n} \\ \frac{1-n}{1+n} \end{bmatrix} \begin{bmatrix} 1 \\ -i \end{bmatrix} = \frac{n-1}{n+1} \begin{bmatrix} 1 \\ i \end{bmatrix}$

both s,p suffer a phase shift of 180° upon reflection

right circ polarized light \uparrow left circ polarized light \uparrow

fresnel relations plots in boole - once past Brewster angle the phase relation changes.

grazing incidence (instead of normal incidence) then Right circ doesn't get converted to left circularly polarized light

$$\begin{bmatrix} A' \\ B' \end{bmatrix} = \begin{bmatrix} e^{-i\delta_s} \\ e^{-i\delta_s} \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = [Ae^{-i\delta_s} + Be^{-i\delta_s}] = e^{-i\delta_s} \begin{bmatrix} A \\ Be^{-i\Delta} \end{bmatrix}$$

arbitrary polarization

simple to understand Jones Matrix

after 2 bounces $\Delta = \pi/2$ in the fresnel rhomb

interference = diffraction = manifestations of wave nature of light.

* fresnel coef at normal $r = \frac{1-n}{1+n} \rightarrow \frac{1-n}{1+n}$ complex of light.

Interference march 26

If you superpose 2 or more waves from a source get intensity square of amplitude
 add amplitudes $\vec{E} = (\vec{E}_1 + \vec{E}_2 + \vec{E}_3 + \dots)$ $I \propto (E)^2$

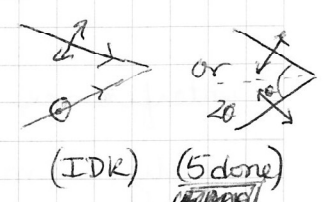
cross-terms give you the interference phenomenon
 2-plane harmonic linearly polarized wave.

$$\vec{E}_1(t) = \vec{E}_1 \exp i(\vec{k}_1 \cdot \vec{r} - \omega t + \phi_1)$$

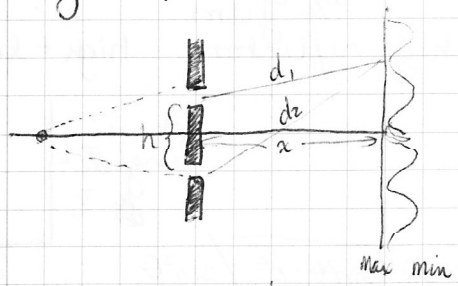
$$\vec{E}_2(t) = \vec{E}_2 \exp i(\vec{k}_2 \cdot \vec{r} - \omega t + \phi_2)$$

$$\phi = (\vec{k}_1 \cdot \vec{r} - \vec{k}_2 \cdot \vec{r} + [\phi_1 - \phi_2])$$

$$I \propto |E|^2 = \vec{E} \cdot \vec{E}^* = |E_1|^2 + |E_2|^2 + 2\vec{E}_1 \cdot \vec{E}_2 \cos \phi$$



Young's Experiment



$$\text{max } k(d_2 - d_1) = \pm 2n\pi \Rightarrow |d_2 - d_1| = n\lambda$$

$$\text{min } \frac{2\pi}{\lambda} |d_2 - d_1| = \pm (n + 1/2) 2\pi \quad |d_2 - d_1| = (n + 1/2)\lambda$$

use Pythagorean Theorem: $d_{\pm} = \sqrt{x^2 + (y \pm h/2)^2}$ $\Delta d = \sqrt{x^2 + (y + h/2)^2} - \sqrt{x^2 + (y - h/2)^2}$
 expand by binomial theorem

$$\Delta d = (x^2 + y^2 + yh + h^2/4)^{1/2} - (x^2 + y^2 - yh + h^2/4)^{1/2}$$

$$= \frac{1}{x} \left[(1 + \frac{y^2}{x^2} + \frac{yh}{x^2} + \frac{h^2}{4x^2})^{1/2} - (1 + \frac{y^2}{x^2} - \frac{yh}{x^2} + \frac{h^2}{4x^2})^{1/2} \right] = \frac{hy}{x} \Leftrightarrow n\lambda$$

$y = 0, \pm n \frac{\lambda x}{h}$ Can you calculate the wavelength of light.

$I = I_1 + I_2 + 2E_1 E_2 \cos \phi$ if the whole pattern moves rapidly up + down eye averages
 $\Delta \phi$ has to have a fixed ϕ value or vary so slowly it drifts very slowly.

$$I = c \langle \vec{E} \cdot \vec{E}^* \rangle = c \langle |E_1|^2 + |E_2|^2 + 2 \text{Re}(\vec{E}_1 \cdot \vec{E}_2^*) \rangle = I_1 + I_2 + 2 \text{Re} \langle \vec{E}_1 \cdot \vec{E}_2^* \rangle$$

$$f = \frac{\int_0^T f(t) dt}{T} \quad \Gamma_{12}(E) = \text{time average of } \langle E_1(t) E_2(t+\tau) \rangle$$

$$\gamma_{12}(\tau) = \frac{\Gamma_{12}(\tau)}{\sqrt{I_1 I_2}} \quad I_{\text{max}} = I_1 + I_2 + 2\sqrt{I_1 I_2} \text{Re} \gamma_{12}$$

$$I_{\text{min}} = I_1 + I_2 - 2\sqrt{I_1 I_2} \text{Re} \gamma_{12}$$

= 0 or 1

$$m = \frac{2\sqrt{I_1 I_2}}{I_1 + I_2} = \text{modulation of interference pattern}$$

$$I_1 = I_2 \therefore m = 1$$

$$I_1 \gg I_2 \therefore$$

if $I_1 = I_2$ complete cancellation $m = 1$

if $I_1 \neq I_2$ $m < 1$ max + min such that the minimums don't go to zero

$$I = (I_1 + I_2) \left(1 - \frac{2\sqrt{I_1 I_2}}{I_1 + I_2} \right)$$

coherence modulation

$$\cos \phi = \pm 1 \left. \begin{array}{l} \text{difference} \\ -1 \end{array} \right\} \frac{4\sqrt{I_1 I_2}}{I_1 + I_2} = 2m$$

11:15

use a beam splitter

$$\Delta \vec{k} = \vec{k}_2 - \vec{k}_1$$



$$\frac{\Delta k/2}{|\vec{k}|} = \sin \theta \quad \text{gives spatial period}$$

$$\Delta k = (k \sin \theta)^2 = \frac{2\pi \sin \theta}{\lambda}$$

crossing angle

$$= \frac{2\pi}{\Lambda}$$

interference period

$$\Lambda = \frac{\lambda}{2 \sin \theta}$$

interference of 2 lasers then combined at $\angle \theta$ spatial distance over which they repeat

$\phi = (k_2 - k_1) \cdot r + \Delta \phi$ gives spatial period of interference pattern

31 March 2009

3.1 3.2 3.6 3.8 3.9 3.12 Optics Homework Due Next Thursday

2nd Midterm Middle of April 7th

Read Handout Ch. 7 of Hetch

Periodic function \rightarrow aperiodic function - FFT

$$I = I_0 = I_2 \quad m = 1 = \frac{2\sqrt{I_1 I_2}}{I_1 + I_2} \quad I = I_T \left[1 + \text{Re} |\delta_{12}| \cos \left(\frac{k_y h}{\lambda} \right) \right] \quad \text{very simple form}$$

$\text{Re} |\delta_{12}|$ Normalized coherence function = 1 for complete coherence close for lasers

$$\langle E_1(t) E_2(t+\tau) \rangle$$

$$I_T = 2I_0$$

$0 \leq \delta_{12} \leq 1 \Rightarrow$ partial coherence

$$I = 2I_0 \left[1 + \text{Re} |\delta_{12}| \cos \left(\frac{k_y h}{\lambda} \right) \right]$$

Shifts in phase in gas tube due to lifetime of excited states, line broadening interference at screen - time difference of arrival at screen interference is washed out because the wave train length \leq path length difference (no contrast)

$\tau =$ time of wave train to exist

Coherence time

$$l_c = c\tau = \text{temporal coherence length or coherence length}$$

$$\Delta E \Delta t \approx \hbar$$

$$E = \hbar \Delta \omega$$

$$\Delta \omega \approx \frac{1}{\tau}$$

$$\tau = \frac{1}{\Delta \omega}$$

$$l_c = c\tau = \frac{c}{\Delta \omega} = \frac{\lambda^2}{2\pi \Delta \lambda}$$

$$\Delta \nu = \frac{c}{\lambda^2} \Delta \lambda$$

$$l_c = \text{coherence length} = \frac{5 \times 10^{-5} \text{ m}}{10^{-8}} = 5 \times 10^{-10} \text{ m}$$

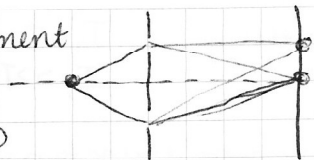
example

max Δ can be to maintain

$$\frac{25 \cdot 10^{-10} \text{ m}}{10^{-8}} \approx 25 \text{ cm}$$



Young's Experiment



longitudinal coherence length

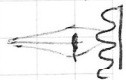
$$\frac{(5.8 \cdot 10^{-5})^2}{3 \cdot 10^{-5}} \approx \frac{25 \cdot 10^{-10}}{3 \cdot 10^{-5}} \approx 8000 \text{ \AA}$$

coherence length is very short
Small path length difference - soon into regime 'no interference'

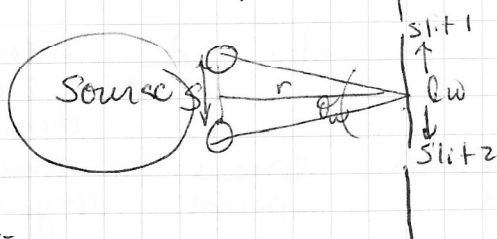
$\sim \frac{|\Delta l|^2}{\Delta \lambda}$ ← central λ
← width of light axes because of finite duration of wave train

monochromatic light $\Delta \lambda \rightarrow 0$ $\Delta \omega \rightarrow 0 \Rightarrow$ nice, complete interference modulation/contrast

Now consider a broader source pinhole $\rightarrow r \rightarrow \infty$
the interference pattern starts losing contrast



$l_w =$ maximum separation between emitting sources.



$$l_w \propto \frac{1}{\theta_w} = \frac{\lambda_{\text{light}}}{\theta_w}$$

$\theta = \frac{s}{r}$ $r =$ distance source to slits $\theta =$ width of source

pinhole $\theta = 0$ and $\Delta \lambda \rightarrow 0$ infinite coherence length

Van Cittert Zernike Theorem = in Born + Wolf = $\frac{1.22 \lambda_{\text{light}}}{\theta_w} = l_w$

if the width is large longitudinal coherence length is small

thermal sources - narrow wavelength light $\lambda = 0.1 \text{ \AA}$

pinhole $\sim .5 \text{ mm} \Rightarrow$ puts limitations on what can be the separation of the slits

holographic gratings - arise from interference Boy! Sheesh!

$$\Lambda = \frac{\lambda}{2 \sin \theta}$$



$E_1 \propto e^{i\vec{k}_1 \cdot \vec{r}}$ $E_2 \propto e^{i\vec{k}_2 \cdot \vec{r}}$
interference
 $e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}}$
spatial frequency

$$\frac{\Delta \vec{k}}{z} = k_1 \sin \theta$$

$$\frac{2\pi}{\Lambda} = \Delta k = 2k_1 \sin \theta = \frac{4\pi}{\lambda} \sin \theta$$

$$\Lambda = \frac{\lambda}{2 \sin \theta}$$

p 401 handout 9.33

to make a grating
interference on a
photoresist
ex. violet/blue light
400nm Argon laser
can make a grating

$$\frac{488}{2 (\sin 30)} = \text{period of grating}$$

p. 62 in book: interference pattern

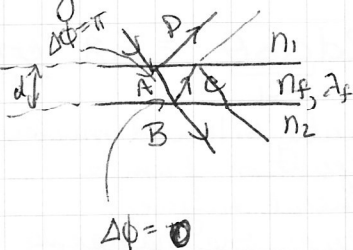


Tuesday April 7, 2009

Interference

2 glass slides - thin film of air (pile of plates)

light source



$$AB = BC = d / \cos \theta_t \quad \lambda_f = \lambda_0 / n_f$$

$$\Delta = n_f [AB + BC] - n_1 AD$$

$$\Delta = 2n_f d \cos \theta_t \quad \text{path length difference}$$

$$d \cos \theta_t = (2m+1) \lambda_f / 4 \Rightarrow 2d \cos \theta_t = (m+1/2) \lambda_f \text{ bright}$$

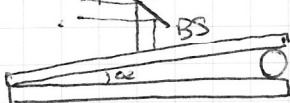
$$2d \cos \theta_t = m \lambda_f \text{ dark}$$

$$2\pi \Delta / \lambda = \delta = \frac{2\pi}{\lambda} (2n_f d \cos \theta_t) \pm \pi$$

δ depends on relative refractive indices

Two Simple Cases

①



Fizeau's fringes

$$d = x \alpha \quad \alpha \text{ in radians}$$

condition for Bragg fringes

$$(m+1/2) \lambda_0 = 2n_f d$$

$$\cos \theta_t \approx 1$$

$$x_m = \frac{(m+1/2) \lambda_f}{2\alpha} \quad \text{condition for the } m\text{th bright fringe's position}$$

$$x_m = \frac{m \lambda_f}{2\alpha} \quad \text{condition position for dark fringe}$$

$$\Delta x = \frac{\lambda_f}{2\alpha}$$

can tell if surfaces aren't flat



② Newton's Rings



$$x^2 = R^2 - (R-d)^2$$

$$x^2 \approx 2Rd$$

$$2n_f d_m = (m+1/2) \lambda_0$$

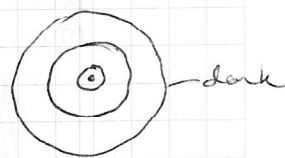
$$x_m = \sqrt{(m+1/2) \lambda_f R} \quad \text{bright fringes} = \sqrt{3/2 \lambda_f R}, \text{ etc.}$$

$$2n_f d = m \lambda \quad \text{central fringe is dark} \Rightarrow x^2 = \frac{m \lambda R}{n_f}$$

$$x = \sqrt{m \lambda_f R}$$



with and without liquid like water



if you know λ_f diameter of rings can measure either bright or dark rings

$\lambda_f = \lambda_0 / n_f$ results can be used for understanding

Michelson Interferometer; example

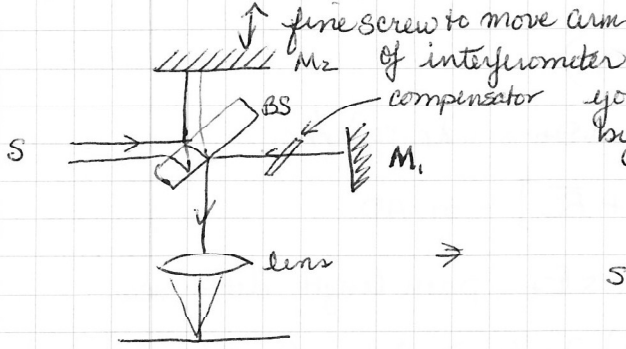
$$\sqrt{3/2 (5 \cdot 10^{-5}) / 10^2} = \sqrt{7.5 \cdot 10^{-3}} \text{ cm}$$

$$\approx 8.6 \cdot 10^{-2} \text{ cm}$$

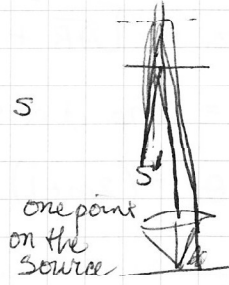
\hat{R} quest inside

$x_1 = 860 \mu\text{m}$ bright fringe

Michaelson Interferometer



you can adjust difference in path by tilting compensator



$$2d \cos \theta = m \lambda \quad \text{condition for maxima}$$

partially silvered mirror reflection from a metal surface each one has same relative phase shift

order of central fringe

$d =$ path length difference

$$m = 4 \cdot 10^3 = \frac{2d}{\lambda} = \frac{2 \cdot 10^4}{5}$$

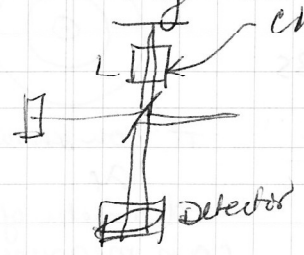
Applications

- can measure λ accurately
- don't look at entire pattern - just look at central fringe ^{w/ PMT, CCD}
- move the arm accurately - count the number of fringes which passed.

$$\left. \begin{aligned} 2d_1 &= m_1 \lambda \\ 2d_2 &= m_2 \lambda \end{aligned} \right\} \text{moving arm}$$

$2(d_2 - d_1) = (m_2 - m_1) \lambda$ number of fringes that go by
can measure $(d_2 - d_1)$ to accuracy of less than micron
So wavelength accuracy is very accurate

- air - quite a few zero's after one once you have vacuum - reads max or min



$$2L(n_{air} - n_{vac}) \quad \text{just use relationship}$$

1,000,005 ← can get n. of gas air

- can measure wavelength differences very accurately

$$2d_1 = m \lambda_1$$

two ring systems

$$\left. \begin{aligned} 2d_1 &= (n + \frac{1}{2}) \lambda_2 \\ 2d_1 &= m \lambda_1 \end{aligned} \right\}$$



max of one falls on min of the other.

$$\left. \begin{aligned} 2d_2 &= (m + 2n + \frac{1}{2}) \lambda \quad \text{dark} \\ 2d_2 &= (n + \Delta n) \lambda_2 \end{aligned} \right\} \text{4 eq's}$$



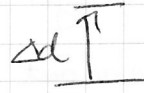
max of one is min of the other. contrast changes

$$\frac{2(d_2 - d_1)}{\lambda_1} = \Delta n + \frac{1}{2}$$

$$\frac{2(d_2 - d_1)}{\lambda_2} = \Delta n - \frac{1}{2}$$

$2\Delta d$ Δd = position between two consecutive loss of contrast conditions
 bright goes to dark and dark goes to bright

$$2\Delta d \left(\frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right) = 1$$



$$2\Delta d \left(\frac{\Delta \lambda}{\lambda^2} \right) = 1$$

$$\Delta \lambda = \frac{\lambda_{av}^2}{2\Delta d}$$

move mirror to where you lose contrast = d_1
 move to next position " " = d_2

λ_{av} = average value of the wavelength

closer $\Delta \lambda$ bigger distance you have to move

example

$$\Delta \lambda \sim 0.1 \text{ \AA} \quad \lambda^2 = 25 \times 10^{10} \text{ cm}^2$$

mirror placement

$$\Delta d \rightarrow 1.25 \text{ cm}$$

between separation b/w closely spaced lenses

Spin-orbit splitting of lines

Thursday

- Coherence Length ω / Michelson Interferometer

- Wedge-shaped path length dif - straight line fringes
 Mirrors not parallel

Anharmonic Waves Periodic Waves Fourier Transforms
 and case where T (period) $\rightarrow \infty$ get a pulse - represent as continuous spectrum of frequency components.

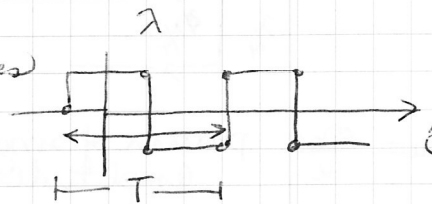
Square, Triangular Waves not pure sines or cosines

If you have a periodic function

$$f(x) = \frac{A_0}{2} + \sum_{m=1}^{\infty} [A_m \cos(kx m) + B_m \sin(mkx)]$$

spatial - λ - wavelength

temporal - T - period



Calculating the coef A_m, B_m

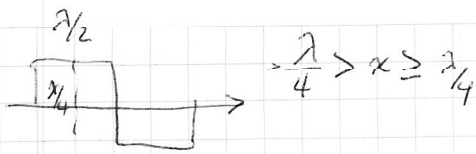
Integrate over a complete period

$$\int_0^{\lambda} f(x) dx = \frac{A_0}{2} \int_0^{\lambda} dx + \sum_{m=1}^{\infty} \int_0^{\lambda} [A_m \cos(kx m) + B_m \sin(mkx)] dx$$

$$= \frac{A_0 \lambda}{2}$$

$$\int_0^{\lambda} \cos^2(mkx) dx = \frac{A_m \lambda}{2} \int_0^{\lambda} (1 + \cos(2mkx)) dx = \frac{A_m \lambda}{2}$$

$$0 = \int_0^{\lambda} f(x) \cos(mkx) dx = \frac{A_0}{2} \int_0^{\lambda} \cos(mkx) dx + \sum_{m=1}^{\infty} \int_0^{\lambda} [A_m \cos^2(mkx) \cos(mkx) + B_m \sin(mkx) \cos(mkx)] dx$$



integrate to get the coefficients

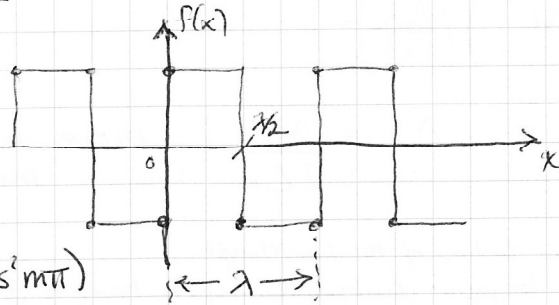
multiply by $\sin(mkx)$ to get the B_m

Simple Example from handout

$$A_0 = \frac{2}{\lambda} \int_0^{\lambda} f(x) dx = 0$$

$$A_m = \frac{2}{\lambda} \int_0^{\lambda} f(x) \cos mkx dx = 0$$

$$B_m = \frac{2}{\lambda} \int_0^{\lambda} f(x) \sin mkx dx = \frac{2}{m\pi} (1 - \cos^2 m\pi)$$



$$f(x) = +1 \quad 0 < x < \lambda/2$$

$$f(x) = -1 \quad \lambda/2 < x < \lambda$$

att. Symmetry about x axis - no A_0

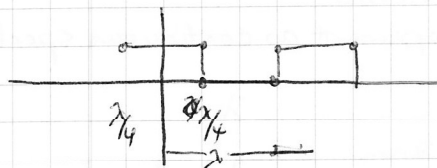
$$f(x) = -f(x)$$

$$\int_0^{\lambda} f(x) dx = 0 \quad \text{one period}$$

Calculate both sin and cos terms

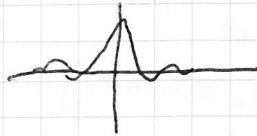
$$f(x) = \frac{4}{\pi} \left(\sin kx + \frac{1}{3} \sin 3kx + \frac{1}{5} \sin 5kx + \dots \right)$$

Starts to approximate the square waveform.



$$f(x) = \frac{2}{a} + \sum_{m=1}^{\infty} \frac{4}{a} \operatorname{sinc}\left(\frac{2\pi m}{a}\right) \cos(mkx)$$

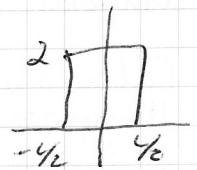
$\operatorname{sinc} = \frac{\sin u}{u}$ pattern of single slit amplitude



$$\frac{2\pi}{\lambda} = k \quad \lambda = \frac{1}{\kappa} \quad \text{Spatial frequency}$$

$$\lambda \rightarrow \infty$$

$$= \frac{1}{\pi} \left[\int_0^{\infty} A(k) \cos kx dk + \int_0^{\infty} B(k) \sin kx dk \right]$$



pulse is even just use $\cos kx$

$$k_p = \frac{2\pi}{\lambda}$$

Euler's Equations

$$e^{i\theta} = \cos\theta + i\sin\theta$$

$$f(x) = \frac{1}{\pi} \int_{-\infty}^{\infty} \cos kx \left[\int_{-\infty}^{\infty} f(x') \cos kx' dx' \right] dk + \frac{1}{\pi} \int_{-\infty}^{\infty} \sin kx \left[\int_{-\infty}^{\infty} f(x') \sin kx' dx' \right] dk$$

ft.

Algebraic relations $e^{i\theta} = \cos\theta + i\sin\theta$ can go from cos to sin

$$f(x) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} [f(x') e^{ikx'}] e^{-ikx} dk$$

called fourier transform pairs

$$f(x) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F(k) e^{-ikx} dk$$

$F(k)$ has both amplitude + phase $F(k) = F(\omega) e^{i\phi(k)}$

The narrower the pulse - the more frequency components you need.

$A_9 = 99\%$ of amplitude ... etc. depends on pulse width

Tuesday April 14, 2009

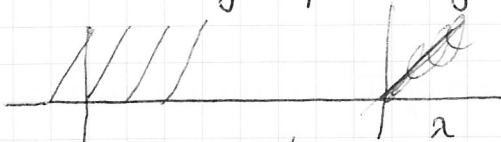
Fourier Series + Fourier Transforms, Relevance in Theory of Optics

$$f(x) = \frac{A_0}{2} + \sum_m [A_m \cos(mkx) + B_m \sin(mkx)]$$

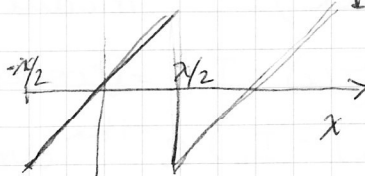
essentially, by the way the function is defined

$$A_m = \int_{-\lambda/2}^{+\lambda/2} f(x) \cos(mkx) dx$$

$$B_m = \int_{-\lambda/2}^{+\lambda/2} f(x) \sin(mkx) dx$$



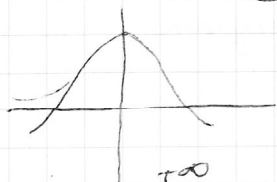
$$f(x) = |x| \quad 0 < x < \lambda$$



$$f(x) = x \quad -\lambda/2 < x < \lambda/2$$

odd function $A_m = 0$

$$f(x) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left[\int_{-\infty}^{+\infty} f(x') e^{ikx'} dx' \right] e^{-ikx} dk = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F(k) e^{-ikx} dk$$

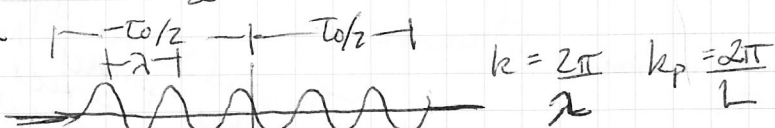


$$f(t) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F(\omega) e^{-i\omega t} d\omega$$

$$F(k) = \int_{-\infty}^{+\infty} f(x) e^{ikx} dx$$

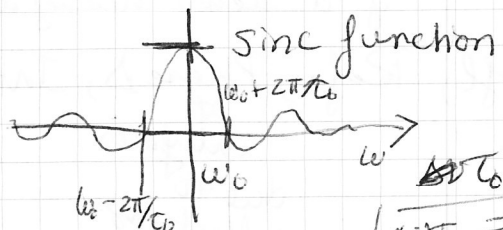
both have
Sym: $\frac{1}{\sqrt{2\pi}}$ vs $\frac{1}{2\pi}$

Fowles wave train



$$f(t) = e^{i\omega_0 t}$$

$$g(\omega) = \sqrt{\frac{2}{\pi}} \frac{\sin(\omega - \omega_0)t_0/2}{(\omega - \omega_0)}$$



$$\Delta \nu t_0 \sim \frac{1}{\Delta \nu}$$

$\Delta \nu t_0 = 1$
Coherence time

$$\Delta \omega = \frac{2\pi}{T}$$

$$\sigma_x \sigma_k \sim 1$$

if you want to create a pulse $\Delta t = \left(\frac{1}{\Delta \nu}\right)$

100 fsec pulse = $\left(\frac{1}{\Delta \nu}\right)$ $\Delta \nu = \frac{1}{10^{-13}} \sim 10^{13} \text{ Hz}$ with a factor of $1.5 - 2$

$\lambda = 800 \text{ nm}$ $\Delta \lambda \sim 30 \text{ nm}$ need to make the short pulse

if you want a short pulse - need a big bandwidth

$$lc = c\tau_0$$

for good temporal coherence, need line width.

narrow wavelengths... on order of a few megahertz for $lc \sim \text{km}$

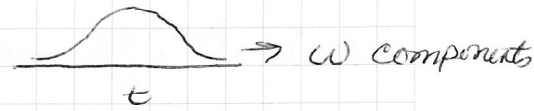
one good use of fourier transforms is Spectroscopy

michaelson interferometer

two arms - one moves broadband IR

in time domain FT \rightarrow frequency domain.

find frequency components



intensity of M.I pattern in book

$$I(x) = I_0 (1 + \cos kx)$$

modulation of I as mirror moves

$$\text{measures} - (I(x) - I_0) = I_0 \cos(kx)$$

p. 81

$$\int (I(x) - I_0) e^{-ikx} dx = I_0 \int (e^{ikx} - e^{-ikx}) dx$$

$$\delta(k - k_0) = \int_{-\infty}^{\infty} e^{i(k_0 - k)x} dx$$

Sample absorbs

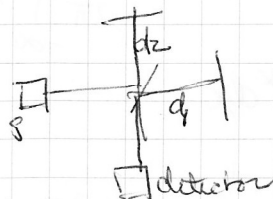
to get absorption
Fourier transform spectroscopy

record interferogram
different get

$$2d = m\lambda$$

$$2|d_2 - d_1| = m\lambda$$

small modulation



exam - use the materials - ask questions
if it seems heavy duty

Thermal Sources depends on geometry - pinhole has perfect coherence extended source
Concept of Temporal Spatial Coherence

Ref, Refr, Phase Δ , Interference of Two Beams

at interfaces due to reflections

Spatial Period Beam Splitter at diff angles here interference patterns

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